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Analysis of the Influence of the Thickness and the Hole Radius on the Calibration Coefficients in the Hole-Drilling Method for the Determination of Non-uniform Residual Stresses

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12 Abstract

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The Hole-Drilling method is a semi-destructive technique useful for obtaining residual stress distributions by drilling and 13measuring relieved strains. The standard for this method, i.e., ASTM E837 - 13a, is based on the Integral Method and 14facilitates obtaining the coefficient matrices required to solve the inverse problem and to calculate the residual stress at 15depths of up to 1.00 mm. A possible deviation from the coefficients given by this standard is searched when the piece has a 16small thickness or the hole diameter is not 2.00 mm. FEM simulations are performed with the aim of analysing these 1718 effects and proposing new matrices, expressions and correlations for conditions outside the usual thickness and diameter 19limits. A parametric sweep over a wide range of thicknesses and hole diameters has been implemented in ANSYS to establish a consistent and automated numerical procedure for widening the applicability of the Hole-Drilling method. 20

21 Keywords Hole-drilling · Residual stress · Finite element method · Strain gauges

23 Introduction

22

Residual stresses are present in many industrial compo-24nents due to fabrication processes. For example, welding 25induces thermal expansion near the heat-affected zone and 26thereby introduces residual stress, which can promote un-27expected failure [1, 2]; machining or cold-forming can also 28generate residual stresses [3] that affect fatigue life [4]. 29However, sometimes, a compressive residual stress distri-30 31bution is introduced with the objective of improving the fatigue life [5–7]. Therefore, knowing the actual stress 3233 state of a piece is fundamental to evaluating its integrity 34during its service life. Measurement techniques can be classified into destructive and non-destructive methods 35 36 [8]. Although the Hole-Drilling method removes material from the target piece, the hole is usually so small in com-37 parison with the piece's dimensions that the component's 38

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² SUCONS Research Group, Escuela Politécnica Superior, Universidad de Burgos, C/Villadiego s/n, 09001 Burgos, Spain integrity is almost unaffected; such measurements may be39regarded as an intermediate situation between destructive40and non-destructive, i.e., semi-destructive [8].41

The Hole-Drilling method comprises three stages: dril-42 ling operation, registration of relieved strains and stress cal-43culation. The relieved strains might be measured using op-44 tical methods, such as Digital Image Correlation or interfer-45ometry [9]. However, those methods have not been 46 standardised in the Hole-Drilling framework; instead, strain 47gauge rosettes are considered in ASTM E837 – 13a [10]. 48 Here, rosettes comprising three strain gauges are analysed, 49but it should be noted that other common configurations 50include a four-gauge rosette (for plasticity correction 51[11–13]) and a special-purpose six-gauge rosette (for mea-52surements requiring high sensitivity [14]). Rosettes of types 53A and B are shown in Fig. 1. Both have two strain gauges 54forming a 90° angle, but while rosette A has the third gauge 55on the prolongation of their bisector, i.e., in the opposite 56quadrant, in rosette B, this third gauge forms a 45° angle 57with the other two, i.e., it is in the same quadrant. 58

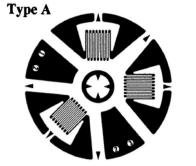
The rosette dimensions are standardised, giving three 59 independent parameters: the rosette diameter D, the gauge 60 length GL and the gauge width GW. The gauge width of a 61 type-B rosette must be less than the GW of a type-A rosette because three strain gauges are placed in the same 63 quadrant. In addition, radii comprising the rosette are 64

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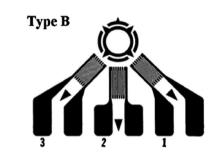
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Fig. 1 Types of 3-strain-gauge rosettes [10]



p =



usually defined, especially for node placement in FiniteElement simulations:

69
$$R_1 = \frac{1}{2}(D - GL)$$
 (1)

$$R_2 = \frac{1}{2}(D + GL)$$
 (2)

70 All the geometric parameters are graphically defined in 74Fig. 4. This paper focuses on the last stage of the Hole-Drilling procedure, i.e., the numerical relationship between 7576 the relieved strains and the actual residual stress distribu-77tion. There are several calculation algorithms whose objective is to relate the relieved strains and the residual stress 78[15]. ASTM E837 – 13a standardises the integral approach 79and establishes a procedure for obtaining the non-uniform 80 residual stresses in the first millimetre of depth. Following 81 82 the standard, a minimum thickness is required for a workpiece to be considered "thick" [10] and for the non-uniform 83 stress calibration coefficients to be valid. 84

The Integral Method is a mathematical approach based on 85 the superposition principle [16]; this algorithm is reviewed in 86 "Results and Discussion" section. The main objective of this 87 study is to discuss the procedure found in ASTM E837 - 13a 88 and to widen its range of applicability. Matrices of calibration 89 90 coefficients are re-evaluated to consider the influences of the thickness and the hole diameter. All calculations are made 91 using Finite Element simulations, and an automated procedure 9293for parametric evaluation is established.

94 Integral Method

The relieved strain registered at drilling depth *h* depends on the stress at depth $\sigma(z)$ and can be found by integrating over every depth increment dz [17]:

$$\varepsilon(h) = \frac{1+\nu}{E} \int_{0}^{h} G(z,h)\sigma(z)dz$$
(3)

where G(z, h) are so-called kernel functions, which quantify 99 the sensitivity of the measured strain to the stress at depth z; 100 the deeper the stress applied is, the lower its influence on the 101 relieved strains measured at the surface. Equation (3) consti-102 tutes an inverse problem: therefore, obtaining the stress distri-103 bution is not straightforward. The Integral Method is based on 104 transforming the continuous problem into a set of discrete 105 equations. Assuming a three-strain-gauge rosette, the follow-106 ing three combinations of strains are usually defined [10]: 107

$$=\frac{\varepsilon_3+\varepsilon_1}{2} \qquad q=\frac{\varepsilon_3-\varepsilon_1}{2} \qquad t=\frac{\varepsilon_3+\varepsilon_1-2\varepsilon_2}{2} \qquad (4)$$

Because the registered strain evolves, these combinations are actually functions of depth or vectors whose components correspond to each step during material removal. The corresponding stress combinations are: 114

$$P = \frac{\sigma_3 + \sigma_1}{2} \qquad Q = \frac{\sigma_3 - \sigma_1}{2} \qquad T = \tau_{13} \tag{5}$$

An integral equation similar to (3) that includes the kernel 116 functions A(z, h) and B(z, h) is defined for each stress-strain 119 pair: 120

$$p(h) = \frac{1+\nu}{E} \int_{0}^{h} A(z,h)P(z)dz$$
(6) 123

$$q(h) = \frac{1}{E} \int_{0}^{h} B(z, h) Q(z) dz$$
(7) 122
126

$$t(h) = \frac{1}{E} \int_{0}^{h} B(z,h)T(z)dz$$
(8) 129
129

To handle this set of inverse problems, the equations are **120** transformed into a discrete matrix system in which p_i , q_i and t_i 131 are the strain combinations obtained experimentally for each 132 depth increment *i* [10]: 133

$$p_i = \frac{1+\nu}{E} \sum_{j=1}^{j=i} \overline{a}_{ij} P_j \tag{9}$$

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$$\begin{array}{ll} 134\\ 139 \end{array} \quad q_i = \frac{1}{E} \sum_{j=1}^{j=i} \overline{b}_{ij} Q_j \end{array} \tag{10}$$

138
$$t_i = \frac{1}{E} \sum_{j=1}^{j=i} \overline{b}_{ij} T_j$$
 (11)

142

140 By solving these three matrix systems, the unknown vectors P_i , Q_i and T_i are found; finally, using the equations in (5), the 144stress distribution can be obtained for each depth *j* in the coor-145146 dinate system defined by the gauges. The non-dimensional coefficients \overline{a}_{ii} and \overline{b}_{ii} represent the strain relaxation after removal 147148 step *i* due to unit stress at depth *j*. They are related to the kernel 149 functions through the following expressions:

$$152 \qquad \overline{a}_{ij} = \int_{z_{j-1}}^{z_j} A(z, h_i) dz \tag{12}$$

$$\begin{array}{ll}
150 & \overline{b}_{ij} = \int\limits_{z_{j-1}}^{z_j} B(z, h_i) dz \\
155 &
\end{array}$$
(13)

156 In the present study, the strain relaxation matrices are examined using FEM simulations. However, sometimes, the cu-157mulative strain relaxation coefficients are found instead. In the 158equi-biaxial situation (i.e., p_i , P_j) the difference in physical 159meaning between \overline{a}_{ii} and \overline{A}_{ii} is shown in Fig. 2. The cumula-160 tive strain relaxation coefficients are defined by [18]: 161

$$\begin{array}{ll}
164 & \overline{A}_{ij} = \int_{0}^{z_j} A(z, h_i) dz \\
163 & \overline{B}_{ij} = \int_{0}^{z_j} B(z, h_i) dz \\
166 & 166 \end{array} \tag{14}$$

Range of Applicability of ASTM E837 – 13a 167

168 Non-uniform stresses can only be calculated for "thick" pieces according to the ASTM standard. The recommended work-169170piece thickness, hole diameter and depth step size are shown 171in Table 1. These values correspond to the most commonly 172used rosettes, types A and B, with a diameter of 5.13 mm:

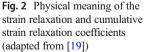


Table 1 Recommendations for workpiece thickness, hole diameter and depth step size in ASTM E837-13a [10]

Max. thickness for a "thin workpiece"	Uniform :	stress	
	Min. D_0	Max. D_0	Step size
1.03	1.52	2.54	0.10
Min. thickness for a "thick workpiece"	Non-unife	orm stress	
	Min. D_0	Max. D_0	Step size
5.13	1.88	2.12	0.05

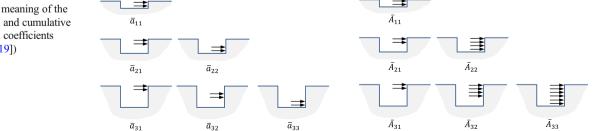
To sum up, when applying the standard the following as-173pects must be considered: 174

- Residual stresses can only be calculated in a 1 mm layer. 175
- Non-uniform stresses can only be calculated for pieces 176
- that are more than 5.13 mm thick. 177Plasticity effects are not included because this standard is 178based on the superposition principle. 179

In addition, the \overline{a}_{ii} and \overline{b}_{ii} matrices are tabulated only for $D_0 =$ 180 2 mm, and a correction factor is introduced for other hole diam-181 eters. Here, possible deviations from this correction are evaluat-182 ed. A discussion of the limitations associated with plasticity is 183 beyond the scope of the present paper; information regarding 184 plastic correction can be found in other studies [12, 20]. 185

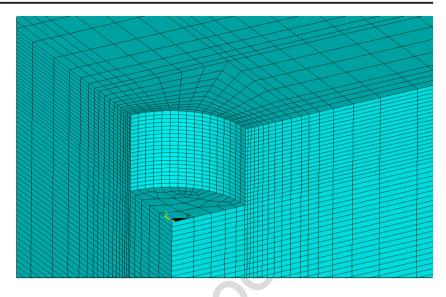
Finite Element Procedure and Validation 186

The Finite Element Method has already been used by many 187 authors for determining \overline{a}_{ii} and \overline{b}_{ii} , the coefficients of the cal-188 ibration matrices [15, 21–25]. The well-known finite elements 189 code ANSYS is used, and a three-dimensional model is cre-190 ated. As a consequence of the symmetry conditions, only a 191 quarter of the model is necessary. An example of the mesh 192 developed is shown in Fig. 3. An element size of 0.05 mm is 193 used in the inner surface of the simulated drilled hole where 194 the loads are applied. Distributed stresses have been applied in 195



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Fig. 3 Simulated drilled hole: Finite Element geometry and mesh



196 0.05-mm increments, following [15]; finer mesh was investi-197 gated but results were practically unaffected so the element size of 0.05 mm is considered for all simulations. A minimum 198 of 16 elements in the hoop direction is used to model a quarter 199 200 of the workpiece. The element type selected is SOLID185, 201 which is commonly used for three-dimensional modelling of 202 solid structures. This element type features plasticity, stress stiffening, large deflection, and large strain capabilities. 203 204 Although in this study, only a linear elastic analysis is required, the model can be used to consider non-linear effects. 205

The main fixed dimensions used for the workpiece simulation are initial diameter of the gauge circle D = 5.13 mm, gauge length GL = 1.59 mm, and external dimension of the workpiece $D_{max} = 12 mm$. The thickness of the workpiece and the diameter of the drilled hole are modified for each simulation with the objective of performing a parametric study. The dimensions are illustrated in Fig. 4.

213The strain measured by the strain gauges is obtained from the radial displacement of the initial and final points of the 214215middle axis of the strain gauge, according to $[u_x(R_2) - u_x(R_1)]/$ 216GL. It must be noted that this measured deformation constitutes a simplification because the gauge width effect is 217218neglected. Additionally, only stresses on the x-y plane have 219been considered; stresses at the hole's bottom face have been 220 neglected, though they can appear due to material removal.

However, the validation presented above demonstrates that the approximation is good enough for calculating the strain based on the strain gauge measurement.

An initial validation analysis is performed. For this purpose, the coefficients obtained for the isotropic stresses \bar{a}_{ij} and for the shear stresses \bar{b}_{ij} are compared with those provided in ASTM E837 – 13a. The obtained Hole-Drilling calibration coefficients in the matrix, \bar{a}_{ij} and \bar{b}_{ij} , are presented in Figs. 5 and 6, respectively, together with the calibration coefficients 229 collected in ASTM E837 – 13a that correspond to a type-B 230 rosette. That type of rosette is chosen for validation because its 231 gauge width is smaller than that of a type-A rosette; therefore, 232 behaviour that is more similar to the present FE simulations is 233 expected. Very good agreement between the coefficients is 234 observed. The results corresponding to intermediate hole 235 depths (h = 0.20 mm, 0.25 mm, etc.) are omitted for clarity. 236

Results and Discussion

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With the aim of assessing the effects of the thickness and the hole 238 radius, a parametric study was conducted. Considering the values 239

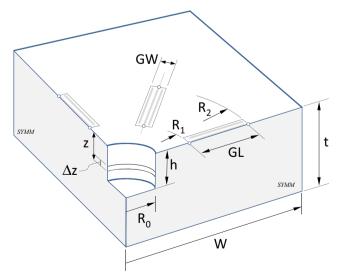
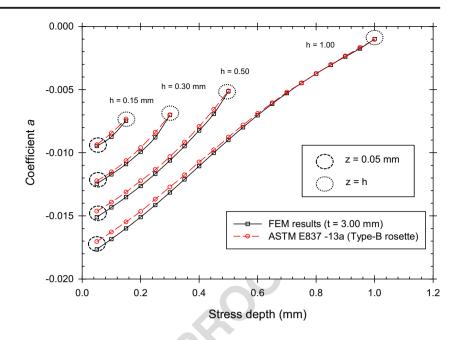


Fig. 4 Main dimensions of the simulated geometry (not to scale)

Fig. 5 Comparison between matrix \overline{a}_{ij} for a type-B rosette (from Table 6(a) in ASTM E837 – 13a) and the FE simulation with $R_0 = 1.00$ mm and thickness = 3.00 mm

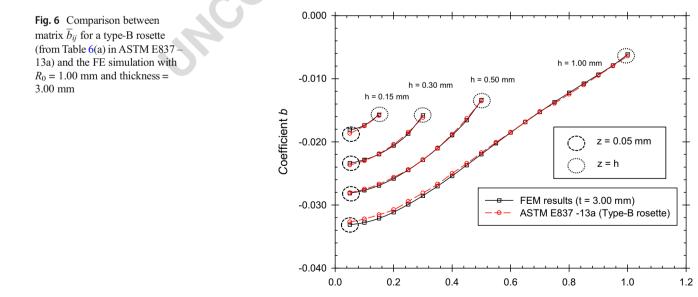


shown in Table 2, a parametric sweep over every possible com-bination was performed, giving a total of 40 simulations.

The results corresponding to a 1.00 mm hole radius and 242a 3.00 mm thickness have already been shown for valida-243244 tion purposes. In the following sections, even though 40 245complete matrices were obtained, only the most substantial 246results are presented. Selected complete matrices for small thicknesses are given in Appendix 1, as the objective of this 247paper is to extend the applicability of ASTM E837-13a 248 249using the matrix Integral Method.

Effect of the Thickness

For a fixed hole radius of 1.00 mm, as in ASTM E837-13a, 251the effect of the thickness on the calibration coefficients 252was evaluated. The graph for all the simulated thicknesses 253shown in Fig. 7 is for the row corresponding to a hole 254depth of 1.00 mm, i.e., the last row of the \overline{a}_{ii} matrix, which 255demonstrates that the trend is asymptotic. This result ex-256 plains why the standard establishes a minimum workpiece 257 thickness, which is equal to a rosette diameter of 5.13 mm, 258



Stress depth (mm)

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 Table 2
 Simulated values of the hole radius and the workpiece thickness

Parameter	Range evaluated
Hole radius: R_0 [mm]	0.25, 0.50, 0.75, 1.00, 1.25
Thickness: t [mm]	1.05, 1.10, 1.25, 1.50, 2.00, 3.00, 5.00, 10

259 as shown in Fig. 7. It is worth noting that for small thicknesses, two different curvatures are obtained in the evolu-260 tion of the effect of the thickness; they depend on whether 261 262 the coefficient corresponds to a stress applied near the bottom of the hole (top lines, near z = 1.00 mm) or next to the 263 workpiece's surface (bottom lines, near z = 0.05 mm). This 264 shape of \overline{a}_{ij} Fig. 7 is caused by the localised bending [26] 265 and the change in behaviour is delimited by the coefficient 266 corresponding to z = 0.60 mm, approximately. This change 267 is attributed to the influence of the free surface at the bot-268 269 tom: for a very low thickness, the constriction associated 270 rwith the bottom is very weak and the deformation in-271 creases to a negative value when stress is applied near 272 z = 0.05 mm (more compression in the strain gauge surface) and even to a positive value when stress is applied 273 274 near z = 1.00 mm (traction at the the surface to which the 275 straing gauge is applied).

For the coefficient line corresponding to z = 0.05 mm, a similar tendency is observed for the values of the \overline{b}_{ij} matrix: compressive deformation increases for low thicknesses because the hole is less constrained. However, due to the association of the \overline{b}_{ij} matrix with a shear stress state, posiExp Mech

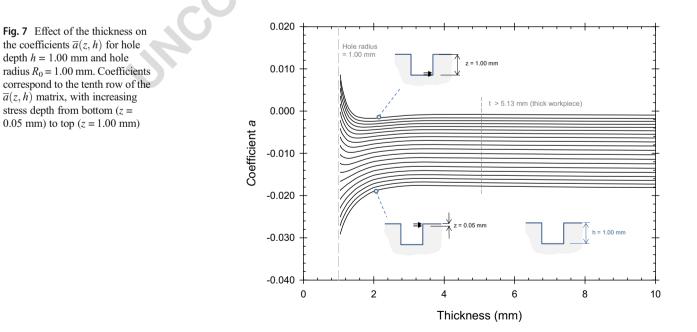
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tive coefficients are not found for z = 1.00 mm and the 281 neighbouring lines. The same curvature is thus found for 282 every coefficient in Fig. 8. 283

For both calibration coefficient matrices, it can be concluded that the thickness limitation of 5.13 mm proposed 285 by the standard is too restrictive. A very smooth coefficient 286 change is found and the values in the standard are only 287 completely invalid for thicknesses less than 3.00 mm. 288 Complete matrices for thicknesses 1.05, 1.50 and 289 2.00 mm are included in Appendix 1. 290

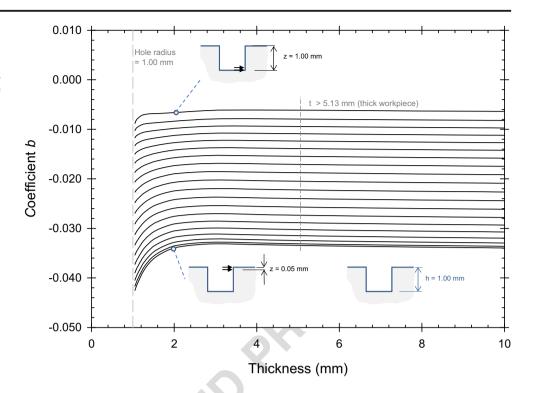
Effect of the Hole Diameter

The hole diameter is determined by the end mill dimen-292sion. Although commercial Hole-Drilling devices feature 293a wide range of cutter diameters, ASTM E837 - 13a 294focuses on a general-purpose 1.00 mm radius for the 295drill, so the applicability of the calibration coefficients 296lies in a range of ± 0.06 mm: R_0 between 0.94 and 2971.06 mm. Figure 9 represents the change in the \overline{a}_{ij} ma-298 trix, with the coefficient corresponding to $R_0 = 1.00$ mm 299 on the x-axis, and the new coefficient for a different 300 radius on the y-axis. Hence, for $R_0 > 1.00$ mm, the 301 points lie below a line with slope one, whereas for R_0 302 < 1.00 mm, the coefficients lie above this line. This 303 result demonstrates how calibration coefficients (or their 304 absolute values) decrease with smaller holes and increase 305 with larger ones. This behaviour may be attributed to the 306 fact that if the ratio D_0/D is very large, the strain is 307 measured close to the edge of the hole, and hence, the 308



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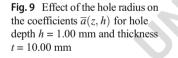
Fig. 8 Effect of the thickness on the coefficients $\overline{b}(z, h)$ for hole depth h = 1.00 mm and hole radius $R_0 = 1.00$ mm. Coefficients correspond to the tenth row of the $\overline{a}(z, h)$ matrix, with increasing stress depth from bottom (z = 0.05 mm) to top (z = 1.00 mm)

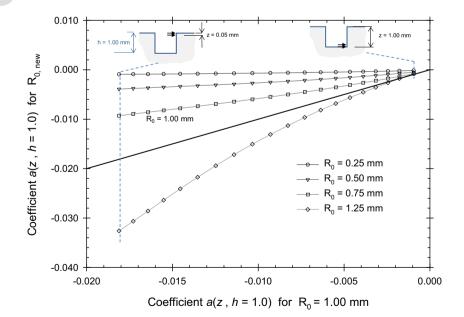


309 deformation must be higher. In a similar way, for $R_0 <$ 310 1.00 mm, the results show that the calibration coeffi-311 cients are less sensitive to the hole size. Again, a bulk 312 constraint may also have a role. It must be recalled that 313 every simulation presented in Figs. 9, 10, 11, and 12 is 314 based on a very thick workpiece (t = 10.00 mm).

315 A similar effect is found for the \overline{b}_{ij} matrix, but an 316 even higher increase in the negative deformation is observed for large values of R_0 . The curves in Figs. 9 and 317 10 are not easy to fit using a linear regression, even 318 though the proposed correction in ASTM E837 – 13a 319 is as follows [10]: 320

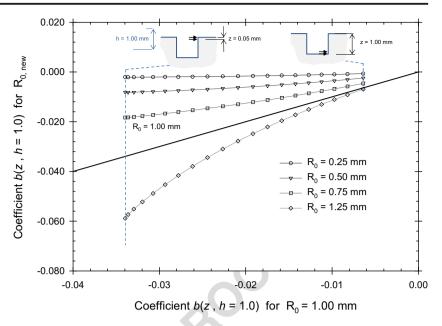
$$\overline{a}_{ij,R_0} = \left(\frac{R_0}{1.00 \text{ mm}}\right)^2 \overline{a}_{ij,1.00 \text{ mm}} \tag{16}$$





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Fig. 10 The effect of the hole radius on the coefficients $\overline{b}(z, h)$ for hole depth h = 1.00 mm and thickness t = 10.00 mm



With the aim of evaluating the apparent deviation of 324325 the simulated coefficients from the correction proposed 326 in equation (16), the ratio $\overline{a}_{R_0}/\overline{a}_{1.00 \text{ mm}}$ is graphed against 327 the hole radius in Fig. 11. The coefficients obtained 328 through FE simulations with different hole sizes are also compared with the correction proposed by the standard, 329 i.e., equation (16). The latter, which is a parabola, is a 330 reasonably good prediction for hole radii near 1.00 mm 331

or for coefficients corresponding to a stress applied near 332 the free surface, i.e., close to z = 0.05 mm. In contrast, 333 coefficients corresponding to a stress applied near the 334 bottom of the hole, i.e., close to z = 1.00 mm, are found 335 to deviate significantly from the correction given in 336 ASTM E837 – 13a. Despite this, the measurements taken 337 during drilling at sub-surface depths are highly suscepti-338 ble to measurement errors, so that deviations in numeri-339

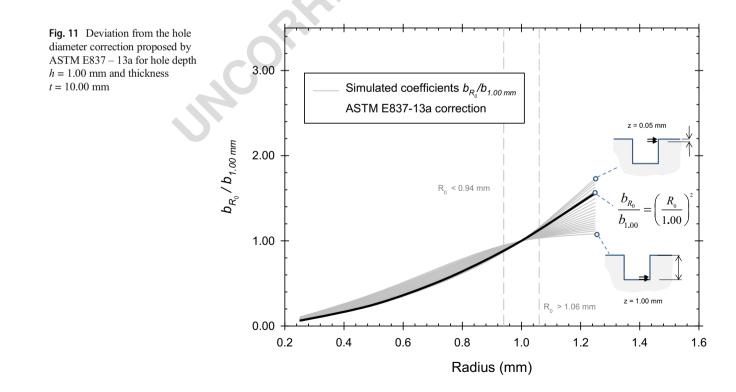
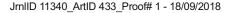
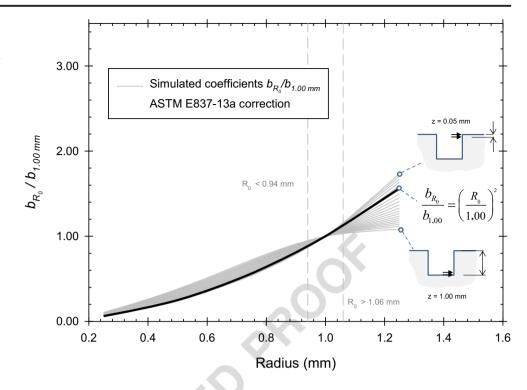


Fig. 12 Deviation from the hole diameter correction proposed by ASTM E837 – 13a for hole depth h = 1.00 mm and thickness t = 10.00 mm





cal values may be acceptable to a certain degree since
their contribution to the overall experimental error is less
than from the measurement errors. The correction by
diameter considered by the standard, although imprecise,
can be valid taking into account that regularization tends
to reduce these effects.

Following the same procedure, Fig. 12 shows a comparison 346 between the simulated values of $\overline{b}_{R_0}/\overline{b}_{1.00 \text{ mm}}$ and the correc-347 tion recommended by the standard. Behaviour similar to that 348 349 found in Fig. 11 is obtained. However, note how coefficients corresponding to different stress locations are concentrated in 350 a narrower spectrum, especially for coefficients close to z =351 1.00 mm. Consequently, it can be assumed here that the pre-352 353 diction given by ASTM E837 - 13a is better for the "b" matrix than for the "a" matrix. 354

355 **Conclusions**

A Finite Element procedure was validated as a powerful
tool for finding coefficient matrices in the Integral
Method framework as a first step in measuring residual
stresses using the Hole-Drilling method. Using ANSYS,
the results were compared with the coefficients given by
ASTM E837 - 13a; they were in very good agreement
for type-B rosettes. It can be deduced from this

correspondence that the present simulations are valid363for thin strain gauges. In future extensions, the gauge364width will be included as an influential parameter.365

In addition, the limits on the thickness and hole radius 366 were studied and discussed. The definition of a "thick" 367 workpiece in ASTM E837 - 13a was attributed to the 368 critical change in the calibration coefficients for small 369 thicknesses, which is physically related to the con-370 straints. The presented results and the matrices given in 371Appendix 1 are expected to overcome this limitation to 372 experimentally determine the non-uniform residual stress 373 distribution in a thin workpiece. The influence of the 374hole diameter was also analysed with a focus on a crit-375ical revision of the correction proposed in ASTM E837 -376 13a. It was concluded that the adjustment for a hole 377 diameter different than 2.00 mm used by the standard 378 might be improved because the coefficients found in 379 the FE simulations deviated significantly from this cor-380 rection. The observed deviation is especially important 381for large hole diameters. As a general conclusion, a par-382 ticular matrix must be obtained through the exposed au-383 tomated numerical procedure when the analysed work-384piece is too thin (t < 3.00 mm) or when the hole diameter 385is relatively large $(D_0 > 1.1 \text{ mm})$. 386

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389 Appendix 1: Matrices for Small Thickness

All calibration matrices correspond to a strain rosette diameter D = 5.13 mm and a hole diameter $D_0 = 2.00$ mm.

Table 3Calibration matrix \overline{a}_{ij} for thickness t = 1.05 mm

Stress	depth									
Hole d	epth									
mm	0.05	0.1	0.15	0.2	0.25	0.3	0.35	0.4	0.45	0.5
0.05	-0.01286									
0.10	-0.01558	-0.01352								
0.15	-0.01789	-0.01614	-0.01379							
0.20	-0.01998	-0.01819	-0.01628	-0.01373						
0.25	-0.02181	-0.02001	-0.01810	-0.01605	-0.01338					
0.30	-0.02339	-0.02156	-0.01967	-0.01765	-0.01550	-0.01277				
0.35	-0.02472	-0.02286	-0.02095	-0.01898	-0.01689	-0.01468	-0.01196			
0.40	-0.02580	-0.02392	-0.02200	-0.02003	-0.01800	-0.01586	-0.01364	-0.01097		
0.45	-0.02665	-0.02475	-0.02283	-0.02087	-0.01885	-0.01678	-0.01463	-0.01242	-0.00984	
0.50	-0.02729	-0.02539	-0.02346	-0.02150	-0.01949	-0.01745	-0.01537	-0.01324	-0.01107	-0.00862
0.55	-0.02774	-0.02584	-0.02392	-0.02196	-0.01997	-0.01794	-0.01589	-0.01383	-0.01174	-0.00964
0.60	-0.02804	-0.02615	-0.02423	-0.02228	-0.02029	-0.01828	-0.01626	-0.01422	-0.01219	-0.01016
0.65	-0.02822	-0.02633	-0.02442	-0.02248	-0.02051	-0.01851	-0.01649	-0.01448	-0.01248	-0.01050
0.70	-0.02832	-0.02643	-0.02453	-0.02259	-0.02063	-0.01864	-0.01664	-0.01464	-0.01265	-0.01069
0.75	-0.02835	-0.02647	-0.02457	-0.02264	-0.02068	-0.01870	-0.01670	-0.01471	-0.01274	-0.01079
0.80	-0.02836	-0.02649	-0.02459	-0.02265	-0.02069	-0.01871	-0.01672	-0.01473	-0.01275	-0.01081
0.85	-0.02839	-0.02650	-0.02459	-0.02266	-0.02069	-0.01870	-0.01670	-0.01470	-0.01272	-0.01076
0.90	-0.02847	-0.02656	-0.02464	-0.02268	-0.02069	-0.01868	-0.01666	-0.01464	-0.01263	-0.01066
0.95	-0.02867	-0.02673	-0.02476	-0.02276	-0.02073	-0.01868	-0.01662	-0.01456	-0.01252	-0.01050
1.00	-0.02911	-0.02709	-0.02505	-0.02298	-0.02088	-0.01875	-0.01662	-0.01449	-0.01237	-0.01027
Stress	depth									
Hole d	epth									
mm	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
0.55	-0.00732									
0.60	-0.00814	-0.00597								
0.65	-0.00853	-0.00660	-0.00457							
0.70	-0.00877	-0.00687	-0.00502	-0.00314						
0.75	-0.00888	-0.00700	-0.00518	-0.00340	-0.00166					
0.80	-0.00890	-0.00703	-0.00521	-0.00344	-0.00173	-0.00010				
0.85	-0.00884	-0.00696	-0.00513	-0.00334	-0.00162	0.00004	0.00156			
0.90	-0.00871	-0.00681	-0.00494	-0.00313	-0.00136	0.00035	0.00198	0.00342		
0.95	-0.00851	-0.00655	-0.00464	-0.00276	-0.00093	0.00086	0.00259	0.00423	0.00562	
1.00	-0.00820	-0.00616	-0.00415	-0.00217	-0.00022	0.00169	0.00357	0.00540	0.00714	0.00856

Exp Mech

Stress	denth									
Hole d	-									
mm	0.05	0.1	0.15	0.2	0.25	0.3	0.35	0.4	0.45	0.5
0.05	-0.01743									
0.10	-0.02040	-0.01865								
0.15	-0.02304	-0.02174	-0.01932							
0.20	-0.02531	-0.02414	-0.02246	-0.01958						
0.25	-0.02748	-0.02636	-0.02484	-0.02276	-0.01947					
0.30	-0.02956	-0.02845	-0.02698	-0.02504	-0.02257	-0.01903				
0.35	-0.03133	-0.03025	-0.02882	-0.02700	-0.02478	-0.02211	-0.01843			
0.40	-0.03295	-0.03189	-0.03050	-0.02874	-0.02665	-0.02425	-0.02147	-0.01769		
0.45	-0.03435	-0.03332	-0.03196	-0.03026	-0.02824	-0.02599	-0.02347	-0.02059	-0.01681	
0.50	-0.03562	-0.03462	-0.03328	-0.03160	-0.02965	-0.02750	-0.02515	-0.02254	-0.01964	-0.01588
0.55	-0.03677	-0.03579	-0.03447	-0.03282	-0.03091	-0.02882	-0.02654	-0.02409	-0.02144	-0.01853
0.60	-0.03780	-0.03684	-0.03554	-0.03391	-0.03203	-0.02997	-0.02775	-0.02540	-0.02291	-0.02027
0.65	-0.03868	-0.03774	-0.03645	-0.03484	-0.03298	-0.03096	-0.02880	-0.02650	-0.02411	-0.02162
0.70	-0.03948	-0.03856	-0.03729	-0.03570	-0.03385	-0.03184	-0.02970	-0.02745	-0.02512	-0.02273
0.75	-0.04013	-0.03924	-0.03799	-0.03642	-0.03460	-0.03261	-0.03051	-0.02829	-0.02600	-0.02367
0.80	-0.04075	-0.03988	-0.03865	-0.03708	-0.03527	-0.03330	-0.03122	-0.02903	-0.02677	-0.02448
0.85	-0.04131	-0.04041	-0.03915	-0.03760	-0.03585	-0.03391	-0.03183	-0.02966	-0.02743	-0.02519
0.90	-0.04178	-0.04092	-0.03966	-0.03813	-0.03636	-0.03441	-0.03235	-0.03021	-0.02802	-0.02581
0.95	-0.04216	-0.04133	-0.04010	-0.03856	-0.03682	-0.03492	-0.03289	-0.03077	-0.02860	-0.02641
1.00	-0.04254	-0.04169	-0.04047	-0.03898	-0.03727	-0.03539	-0.03337	-0.03126	-0.02911	-0.02695
Stress	depth				C					
Hole d	epth									
mm	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
0.55	-0.01488									
0.60	-0.01743	-0.01390								
0.65	-0.01903	-0.01629	-0.01292							
0.70	-0.02029	-0.01780	-0.01517	-0.01201						
0.75	-0.02132	-0.01896	-0.01657	-0.01409	-0.01114					
0.80	-0.02219	-0.01991	-0.01764	-0.01539	-0.01309	-0.01039				
0.85	-0.02294	-0.02073	-0.01854	-0.01640	-0.01428	-0.01214	-0.00969			
0.90	-0.02361	-0.02144	-0.01932	-0.01725	-0.01524	-0.01328	-0.01134	-0.00921		
0.95	-0.02423	-0.02209	-0.02000	-0.01799	-0.01604	-0.01417	-0.01239	-0.01068	-0.00885	
1.00	-0.02480	-0.02270	-0.02066	-0.01870	-0.01681	-0.01502	-0.01331	-0.01172	-0.01026	-0.00882

AUTIPIC Rub S3 Port O 16/09P018

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Fxn	Mech

Stress	depth									
Hole d	epth									
mm	0.05	0.1	0.15	0.2	0.25	0.3	0.35	0.4	0.45	0.5
0.05	-0.00913									
0.10	-0.01101	-0.00968								
0.15	-0.01258	-0.01154	-0.00995							
0.20	-0.01402	-0.01296	-0.01178	-0.01000						
0.25	-0.01530	-0.01425	-0.01310	-0.01178	-0.00986					
0.30	-0.01644	-0.01538	-0.01426	-0.01299	-0.01157	-0.00956				
0.35	-0.01744	-0.01637	-0.01525	-0.01404	-0.01268	-0.01118	-0.00915			
0.40	-0.01831	-0.01723	-0.01610	-0.01490	-0.01361	-0.01219	-0.01066	-0.00864		
0.45	-0.01905	-0.01796	-0.01683	-0.01564	-0.01437	-0.01302	-0.01157	-0.01004	-0.00806	
0.50	-0.01967	-0.01857	-0.01744	-0.01625	-0.01500	-0.01368	-0.01230	-0.01085	-0.00934	-0.00744
0.55	-0.02019	-0.01908	-0.01794	-0.01676	-0.01551	-0.01422	-0.01287	-0.01149	-0.01006	-0.00859
0.60	-0.02060	-0.01949	-0.01836	-0.01717	-0.01593	-0.01464	-0.01332	-0.01197	-0.01061	-0.00922
0.65	-0.02094	-0.01982	-0.01869	-0.01750	-0.01627	-0.01499	-0.01368	-0.01235	-0.01102	-0.00970
0.70	-0.02119	-0.02008	-0.01894	-0.01776	-0.01653	-0.01526	-0.01396	-0.01265	-0.01134	-0.01004
0.75	-0.02139	-0.02028	-0.01914	-0.01796	-0.01673	-0.01546	-0.01417	-0.01287	-0.01158	-0.01030
0.80	-0.02154	-0.02043	-0.01929	-0.01811	-0.01688	-0.01562	-0.01433	-0.01304	-0.01176	-0.01050
0.85	-0.02164	-0.02053	-0.01939	-0.01822	-0.01699	-0.01573	-0.01445	-0.01316	-0.01189	-0.01064
0.90	-0.02171	-0.02060	-0.01947	-0.01829	-0.01707	-0.01581	-0.01454	-0.01325	-0.01198	-0.01074
0.95	-0.02175	-0.02065	-0.01951	-0.01834	-0.01712	-0.01587	-0.01459	-0.01331	-0.01204	-0.01081
1.00	-0.02177	-0.02067	-0.01954	-0.01837	-0.01715	-0.01590	-0.01462	-0.01335	-0.01208	-0.01085
Stress	depth									
Hole d	epth									
mm	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
0.55	-0.00679									
0.60	-0.00781	-0.00613								
0.65	-0.00836	-0.00703	-0.00548							
0.70	-0.00877	-0.00750	-0.00626	-0.00483						
0.75	-0.00906	-0.00785	-0.00666	-0.00549	-0.00419					
0.80	-0.00927	-0.00808	-0.00694	-0.00583	-0.00475	-0.00357				
0.85	-0.00942	-0.00826	-0.00714	-0.00606	-0.00503	-0.00404	-0.00297			
0.90	-0.00953	-0.00838	-0.00727	-0.00622	-0.00522	-0.00426	-0.00334	-0.00238		
0.95	-0.00961	-0.00846	-0.00736	-0.00632	-0.00533	-0.00440	-0.00351	-0.00267	-0.00180	
1.00	-0.00965	-0.00851	-0.00741	-0.00638	-0.00540	-0.00448	-0.00361	-0.00279	-0.00200	-0.00123

Exp Mech

Stress d	lenth									
Hole de										
mm	0.05	0.1	0.15	0.2	0.25	0.3	0.35	0.4	0.45	0.5
0.05	-0.01508									
0.10	-0.01759	-0.01625								
0.15	-0.01965	-0.01874	-0.01690							
0.20	-0.02172	-0.02092	-0.01967	-0.01728						
0.25	-0.02365	-0.02287	-0.02167	-0.01998	-0.01725					
0.30	-0.02531	-0.02457	-0.02350	-0.02199	-0.01996	-0.01696				
0.35	-0.02682	-0.02611	-0.02509	-0.02370	-0.02191	-0.01972	-0.01653			
0.40	-0.02819	-0.02749	-0.02650	-0.02516	-0.02350	-0.02153	-0.01920	-0.01593		
0.45	-0.02944	-0.02875	-0.02775	-0.02646	-0.02490	-0.02307	-0.02095	-0.01850	-0.01524	
0.50	-0.03047	-0.02982	-0.02887	-0.02760	-0.02607	-0.02434	-0.02240	-0.02022	-0.01773	-0.01446
0.55	-0.03143	-0.03080	-0.02986	-0.02862	-0.02713	-0.02545	-0.02359	-0.02156	-0.01932	-0.01683
0.60	-0.03227	-0.03166	-0.03074	-0.02951	-0.02805	-0.02641	-0.02461	-0.02266	-0.02057	-0.01832
0.65	-0.03303	-0.03242	-0.03151	-0.03031	-0.02885	-0.02724	-0.02548	-0.02359	-0.02158	-0.01948
0.70	-0.03367	-0.03308	-0.03218	-0.03099	-0.02955	-0.02796	-0.02623	-0.02437	-0.02242	-0.02040
0.75	-0.03424	-0.03366	-0.03277	-0.03158	-0.03016	-0.02859	-0.02688	-0.02505	-0.02314	-0.02118
0.80	-0.03472	-0.03416	-0.03328	-0.03210	-0.03069	-0.02913	-0.02744	-0.02563	-0.02375	-0.02183
0.85	-0.03515	-0.03460	-0.03373	-0.03256	-0.03116	-0.02961	-0.02793	-0.02614	-0.02429	-0.02239
0.90	-0.03552	-0.03498	-0.03412	-0.03296	-0.03156	-0.03002	-0.02836	-0.02658	-0.02474	-0.02287
0.95	-0.03584	-0.03531	-0.03446	-0.03330	-0.03192	-0.03038	-0.02873	-0.02696	-0.02514	-0.02328
1.00	-0.03612	-0.03559	-0.03475	-0.03360	-0.03222	-0.03069	-0.02905	-0.02729	-0.02548	-0.02364
Stress c	lepth									
Hole de	epth									
mm	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
0.55	-0.01364									
0.60	-0.01587	-0.01280								
0.65	-0.01727	-0.01491	-0.01196							
0.70	-0.01833	-0.01618	-0.01391	-0.01112						
0.75	-0.01919	-0.01718	-0.01512	-0.01296	-0.01033					
0.80	-0.01989	-0.01796	-0.01602	-0.01406	-0.01202	-0.00954				
0.85	-0.02050	-0.01862	-0.01676	-0.01491	-0.01306	-0.01114	-0.00881			
0.90	-0.02100	-0.01915	-0.01734	-0.01557	-0.01382	-0.01208	-0.01028	-0.00811		
0.95	-0.02143	-0.01962	-0.01784	-0.01611	-0.01443	-0.01279	-0.01116	-0.00947	-0.00746	
1.00	-0.02180	-0.02001	-0.01826	-0.01657	-0.01493	-0.01335	-0.01180	-0.01027	-0.00871	-0.00684

AUTIPIC Rub S3 Port O 16/09P018

F	NA I.
Exp	Mech

Stress	depth									
Hole d	-									
mm	0.05	0.1	0.15	0.2	0.25	0.3	0.35	0.4	0.45	0.5
0.05	-0.00751									
0.10	-0.00909	-0.00800								
0.15	-0.01041	-0.00960	-0.00825							
0.20	-0.01162	-0.01080	-0.00985	-0.00829						
0.25	-0.01271	-0.01190	-0.01097	-0.00987	-0.00816					
0.30	-0.01369	-0.01286	-0.01197	-0.01092	-0.00971	-0.00789				
0.35	-0.01455	-0.01372	-0.01283	-0.01184	-0.01069	-0.00939	-0.00753			
0.40	-0.01532	-0.01447	-0.01358	-0.01261	-0.01153	-0.01031	-0.00896	-0.00709		
0.45	-0.01598	-0.01513	-0.01424	-0.01327	-0.01221	-0.01107	-0.00980	-0.00844	-0.00660	
0.50	-0.01656	-0.01569	-0.01480	-0.01383	-0.01280	-0.01168	-0.01050	-0.00921	-0.00786	-0.0060
0.55	-0.01705	-0.01618	-0.01528	-0.01432	-0.01329	-0.01219	-0.01104	-0.00984	-0.00857	-0.0072
0.60	-0.01746	-0.01659	-0.01568	-0.01472	-0.01370	-0.01261	-0.01148	-0.01032	-0.00912	-0.0078
0.65	-0.01781	-0.01693	-0.01602	-0.01506	-0.01404	-0.01296	-0.01185	-0.01071	-0.00955	-0.0083
0.70	-0.01809	-0.01721	-0.01630	-0.01534	-0.01432	-0.01325	-0.01215	-0.01102	-0.00988	-0.0087
0.75	-0.01833	-0.01745	-0.01654	-0.01557	-0.01456	-0.01349	-0.01239	-0.01127	-0.01015	-0.0090
0.80	-0.01852	-0.01764	-0.01673	-0.01576	-0.01475	-0.01368	-0.01259	-0.01148	-0.01037	-0.0092
0.85	-0.01868	-0.01779	-0.01688	-0.01592	-0.01490	-0.01384	-0.01275	-0.01164	-0.01054	-0.0094
0.90	-0.01880	-0.01792	-0.01700	-0.01604	-0.01502	-0.01396	-0.01287	-0.01177	-0.01067	-0.0096
0.95	-0.01890	-0.01801	-0.01710	-0.01613	-0.01512	-0.01406	-0.01297	-0.01187	-0.01078	-0.0097
1.00	-0.01897	-0.01809	-0.01717	-0.01621	-0.01519	-0.01414	-0.01305	-0.01195	-0.01086	-0.0098
Stress	depth				C					
Hole d	epth									
mm	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
0.55	-0.00556									
0.60	-0.00662	-0.00503								
0.65	-0.00719	-0.00600	-0.00452							
0.70	-0.00763	-0.00651	-0.00539	-0.00403						
0.75	-0.00796	-0.00690	-0.00585	-0.00481	-0.00357					
0.80	-0.00821	-0.00718	-0.00618	-0.00521	-0.00426	-0.00314				
0.85	-0.00840	-0.00739	-0.00643	-0.00551	-0.00461	-0.00375	-0.00274			
0.90	-0.00856	-0.00756	-0.00661	-0.00571	-0.00487	-0.00405	-0.00327	-0.00237		
0.95	-0.00868	-0.00769	-0.00675	-0.00587	-0.00504	-0.00427	-0.00353	-0.00283	-0.00203	
1.00	-0.00877	-0.00778	-0.00686	-0.00599	-0.00517	-0.00442	-0.00371	-0.00305	-0.00242	-0.0017

Exp Mech

Table 8	Calibration	n matrix \overline{b}_{ij} for	thickness $t = 2$	2.00 mm						
Stress c	-									
Hole de	epth									
mm	0.05	0.1	0.15	0.2	0.25	0.3	0.35	0.4	0.45	0.5
0.05	-0.01414									
0.10	-0.01653	-0.01532								
0.15	-0.01846	-0.01768	-0.01598							
0.20	-0.02043	-0.01976	-0.01864	-0.01638						
0.25	-0.02226	-0.02161	-0.02055	-0.01898	-0.01637					
0.30	-0.02384	-0.02323	-0.02230	-0.02091	-0.01899	-0.01611				
0.35	-0.02526	-0.02469	-0.02380	-0.02253	-0.02086	-0.01878	-0.01570			
0.40	-0.02654	-0.02598	-0.02512	-0.02391	-0.02237	-0.02053	-0.01831	-0.01514		
0.45	-0.02773	-0.02717	-0.02631	-0.02515	-0.02371	-0.02199	-0.01999	-0.01765	-0.01448	
0.50	-0.02870	-0.02818	-0.02736	-0.02623	-0.02482	-0.02320	-0.02138	-0.01930	-0.01691	-0.01374
0.55	-0.02960	-0.02910	-0.02829	-0.02718	-0.02581	-0.02425	-0.02250	-0.02058	-0.01844	-0.01605
0.60	-0.03040	-0.02991	-0.02912	-0.02803	-0.02668	-0.02516	-0.02347	-0.02162	-0.01963	-0.01748
0.65	-0.03109	-0.03062	-0.02984	-0.02876	-0.02743	-0.02593	-0.02429	-0.02250	-0.02059	-0.01859
0.70	-0.03168	-0.03123	-0.03046	-0.02939	-0.02808	-0.02660	-0.02499	-0.02324	-0.02138	-0.01946
0.75	-0.03221	-0.03176	-0.03101	-0.02995	-0.02864	-0.02719	-0.02559	-0.02387	-0.02206	-0.02019
0.80	-0.03266	-0.03222	-0.03148	-0.03043	-0.02913	-0.02769	-0.02611	-0.02441	-0.02263	-0.02080
0.85	-0.03305	-0.03262	-0.03188	-0.03084	-0.02956	-0.02812	-0.02655	-0.02487	-0.02311	-0.02131
0.90	-0.03339	-0.03297	-0.03224	-0.03120	-0.02992	-0.02850	-0.02694	-0.02527	-0.02353	-0.02175
0.95	-0.03369	-0.03328	-0.03255	-0.03152	-0.03025	-0.02883	-0.02728	-0.02561	-0.02388	-0.02212
1.00	-0.03394	-0.03353	-0.03281	-0.03178	-0.03052	-0.02910	-0.02756	-0.02591	-0.02419	-0.02244
Stress of	lepth									
Hole de	epth									
mm	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
0.55	-0.01297									
0.60	-0.01513	-0.01216								
0.65	-0.01647	-0.01420	-0.01137	X						
0.70	-0.01749	-0.01544	-0.01327	-0.01058						
0.75	-0.01830	-0.01638	-0.01442	-0.01236	-0.00984					
0.80	-0.01896	-0.01712	-0.01527	-0.01341	-0.01147	-0.00911				
0.85	-0.01951	-0.01772	-0.01595	-0.01420	-0.01244	-0.01063	-0.00843			
0.90	-0.01997	-0.01821	-0.01649	-0.01481	-0.01316	-0.01151	-0.00982	-0.00778		
0.95	-0.02036	-0.01864	-0.01695	-0.01531	-0.01372	-0.01217	-0.01064	-0.00907	-0.00718	
1.00	-0.02070	-0.01899	-0.01732	-0.01572	-0.01417	-0.01268	-0.01123	-0.00981	-0.00835	-0.00662

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